



دانشگاه یزد

Yazd Univ.

Computational
Geometry

Course Outline

Textbook

Grading

Prerequisites

Introduction

What is CG?

Research on CG

Journals

Conferences

Computational Geometry (Master Course)

Mohammad Farshi

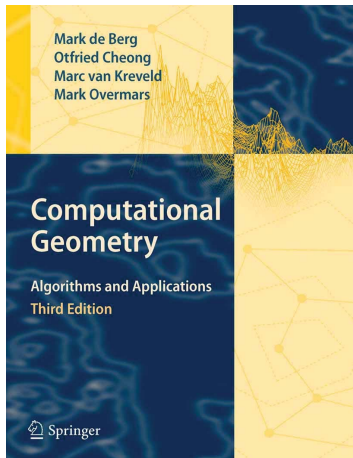
Department of Computer Science,
Yazd University

1393-1



Textbook:

Mark de Berg, Otfried Cheong, Marc van Kreveld, Mark Overmars, **Computational Geometry Algorithms and Applications**, 3rd Edition, Springer-Verlag Berlin Heidelberg, 2008.



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Grading:

- Midterm exam: 6
- Final exam: 7
- Presentation: 3
- Homework: 4
- **Important:** For passing the course, one should get at least 8 from midterm+final exams.





CG on Web:

- **Course Webpage:**
cs.yazd.ac.ir/farshi/Teaching/CG3931/CG.html
- **(Jeff Erickson)**
compgeom.cs.uiuc.edu/~jeffe/compgeom/courses.html
- **(David Eppstein)** www.ics.uci.edu/~eppstein/geom.html
- **(Godfried Toussaint)**
www-cgri.cs.mcgill.ca/~godfried/teaching/cg-web.html
- **Computational Geometry Pages**
www.computational-geometry.org
- and much more ...



What you need to know:

- **Basic Algorithms and Algorithm Analysis:** $\mathcal{O}$, Θ notations, sorting, searching.
- **Basic Data Structures:** Priority Queue (Heap), Binary Search Tree, ... and their analysis.
- **Basic Probability theory:** Expected value, ...
- **Not needed:** Application of CG, programming, knowledge in Geometry.

Prerequisites:



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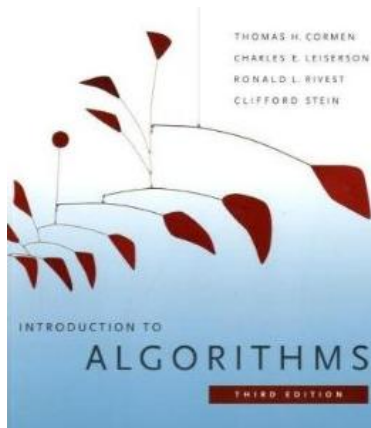
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Computational Geometry

- is a branch of computer science devoted to the study of algorithms which can be stated in terms of geometry.
- is a subfield of the Design and Analysis of Algorithms
- deals with efficient data structures and algorithms for geometric problems
- is only about 30 years old
- started out by developing solid theoretical foundations, but became more and more applied over the last years



What is CG?



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Applications

- Computer graphics,
- Computer-aided design and manufacturing (CAD/CAM),
- Robotics (motion planning and visibility problems),
- Geographic Information Systems (GIS) (geometrical location and search, route planning),
- Integrated Circuit design (IC geometry design and verification),
- and so on.



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The main branches of computational geometry are:

- **Combinatorial computational geometry**, also called **algorithmic geometry**, which deals with geometric objects as discrete entities. A groundlaying book in the subject by Preparata and Shamos dates the first use of the term "computational geometry" in this sense by 1975.
- **Numerical computational geometry**, also called **machine geometry**, computer-aided geometric design (CAGD), or geometric modeling, which deals primarily with representing real-world objects in forms suitable for computer computations in CAD/CAM systems. This branch may be seen as a further development of descriptive geometry and is often considered a branch of computer graphics or CAD.

What is CG?



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Combinatorial computational geometry

- The primary goal is to develop *efficient algorithms* and *data structures* for *solving problems* stated in terms of basic geometrical objects: points, line segments, polygons, polyhedra, etc.
- Example: **The closest pair problem**: Given n points in the plane, find the two with the smallest distance from each other. The brute-force algorithm takes $\mathcal{O}(n^2)$ time. A classic result: an algorithm that takes $\mathcal{O}(n \log n)$ time. Also randomized algorithms that take $\mathcal{O}(n)$ expected time, as well as a deterministic algorithm that takes $\mathcal{O}(n \log \log n)$ time.
- Computational geometry focuses heavily on *computational complexity* since the algorithms are meant to be used on very large data sets containing tens or hundreds of millions of points.

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Problem classes

- Static problems
 - 1 **Convex hull:** Given a set of points, find the smallest convex polyhedron/polygon containing all the points.
 - 2 **Line segment intersection:** Find the intersections between a given set of line segments.
 - 3 **Voronoi diagram:** Given a set of points, partition the space according to which point is closest.
 - 4 **Closest pair of points:** Given a set of points, find the two with the smallest distance from each other.
 - 5 **Euclidean shortest path:** Connect two points in a Euclidean space (with polyhedral obstacles) by a shortest path.
 - 6 **Polygon triangulation:** Given a polygon, partition its interior into triangles

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Problem classes

- Geometric query problems
 - 1 **Range searching:** Preprocess a set of points, in order to efficiently count the number of points inside a query region.
 - 2 **Point location:** Given a partitioning of the space into cells, produce a data structure that efficiently tells in which cell a query point is located.
 - 3 **Nearest neighbor:** Preprocess a set of points, in order to efficiently find which point is closest to a query point.
 - 4 **Ray tracing:** Given a set of objects in space, produce a data structure that efficiently tells which object a query ray intersects first.

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Problem classes

- Dynamic problems
- Variations
 - Point in polygon: Decide whether a point is inside or outside a given polygon.



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Journals

- 1 Computational Geometry: Theory and Applications (CGTA)
- 2 Discrete & Computational Geometry (DCG)
- 3 International Journal of Computational Geometry and Applications (IJCGA)
- 4 Journal of Computational Geometry (NEW)
- 5 Other algorithmic journals



Conferences

- 1 ACM Symposium on Computational Geometry (SOCG)
- 2 Canadian Conference on Computational Geometry (CCCG)
- 3 European Workshop on Computational Geometry (EWCG)
- 4 International Conference on Computational Geometry and Computer Vision
- 5 Others, like SODA, STOC, ESA.



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